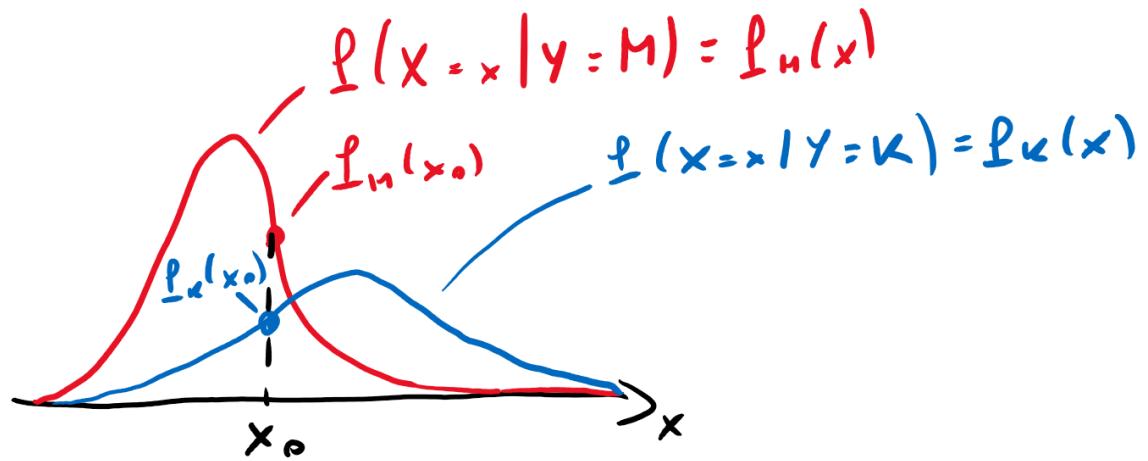


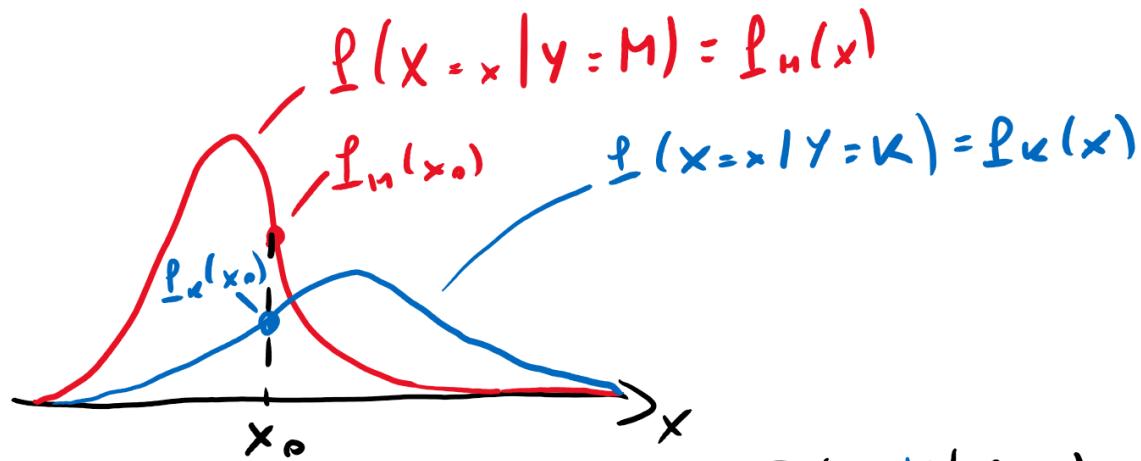
$$P(Y=M) = \pi_M$$

$$P(Y=K) = \pi_K$$



$$P(y=M) = \bar{\pi}_M = \frac{N_M}{N}$$

$$P(y=K) = \bar{\pi}_K = \frac{N_K}{N}$$

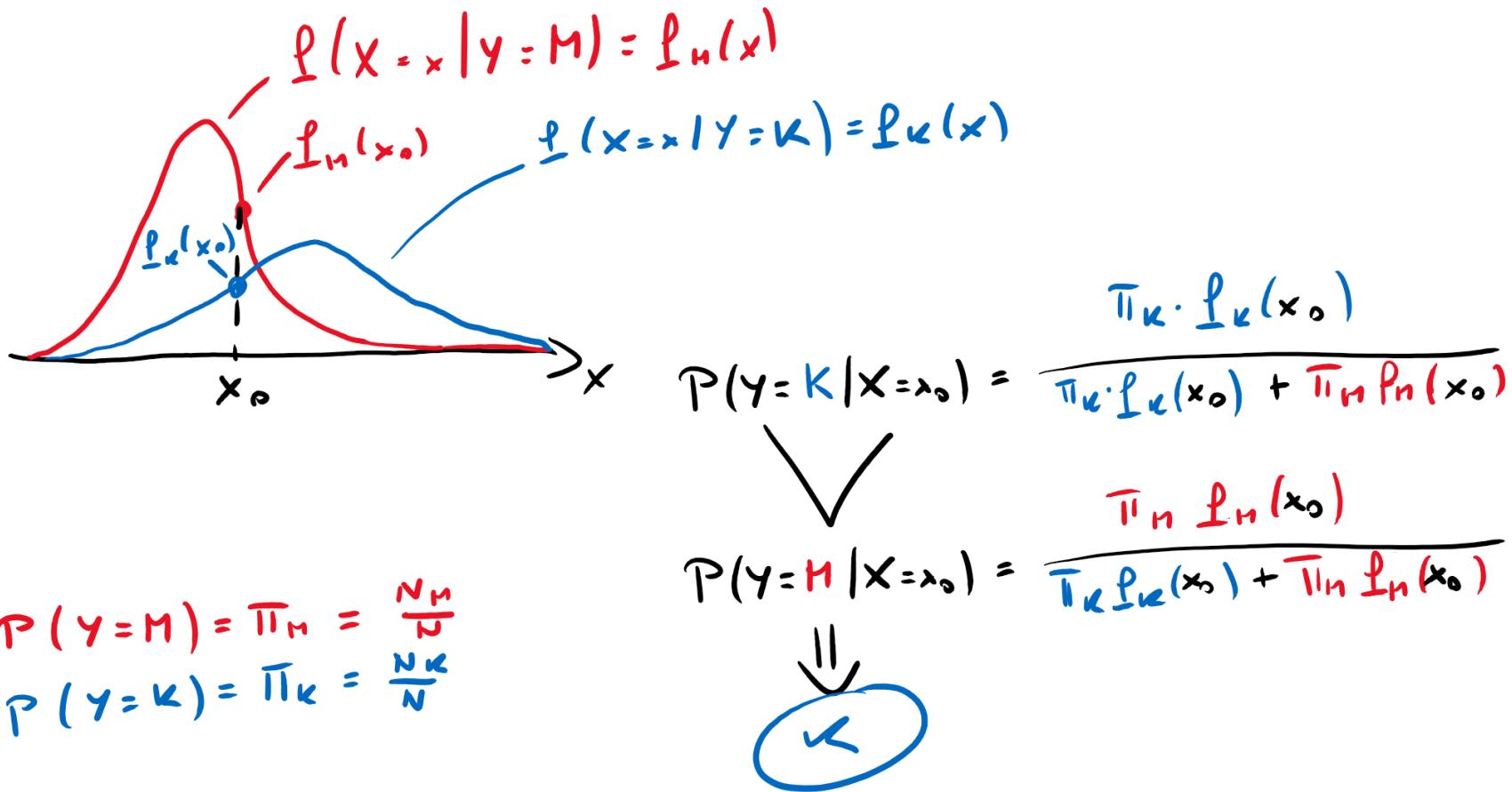


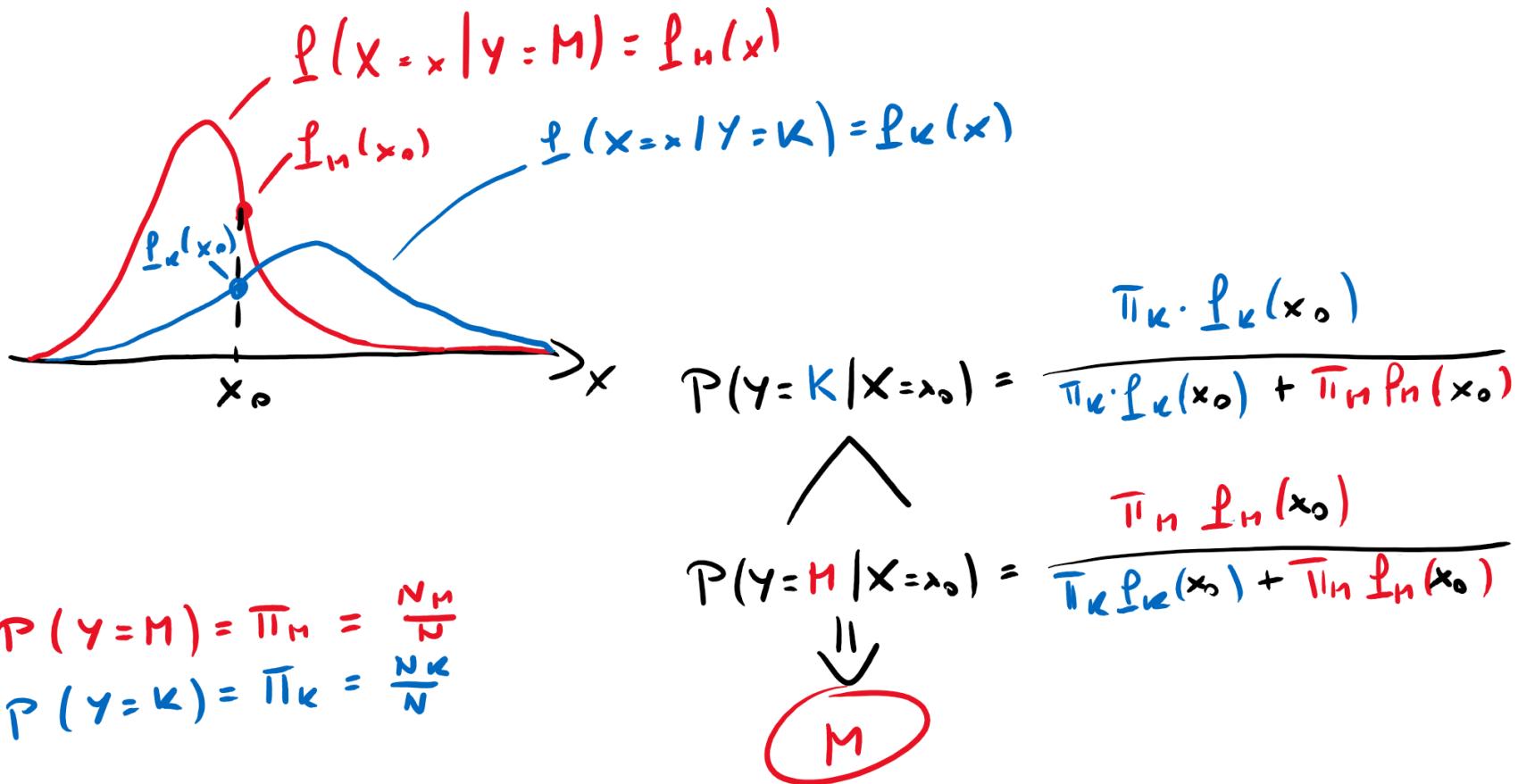
$$P(Y=K | X=x_0) = \frac{\pi_K \cdot P_K(x_0)}{\pi_K \cdot P_K(x_0) + \pi_M P_M(x_0)}$$

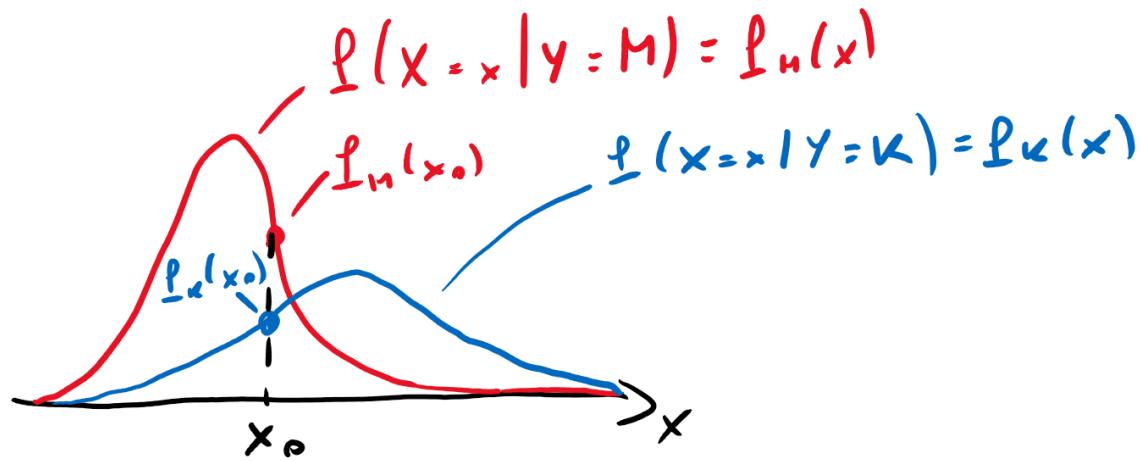
$$P(Y=M | X=x_0) = \frac{\pi_M P_M(x_0)}{\pi_K P_K(x_0) + \pi_M P_M(x_0)}$$

$$P(Y=M) = \pi_M = \frac{N_M}{N}$$

$$P(Y=K) = \pi_K = \frac{N_K}{N}$$



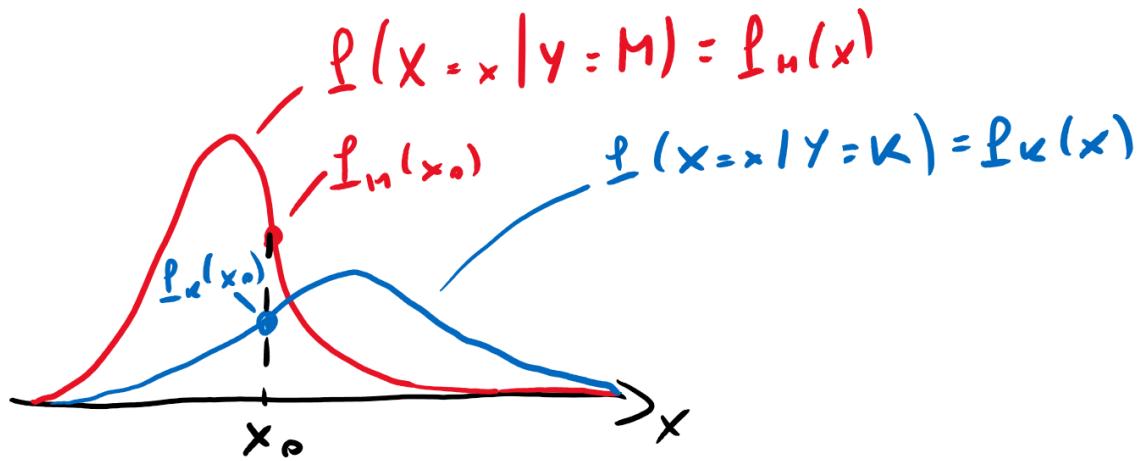




$$\pi_K \cdot P_K(x_0) > \pi_M P_M(x_0) \Rightarrow K$$

$$P(y=M) = \pi_M = \frac{N_M}{N}$$

$$P(y=K) = \pi_K = \frac{N_K}{N}$$

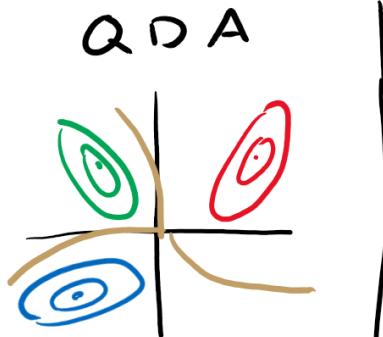


$$\pi_K \cdot P_K(x_0) < \pi_M P_M(x_0) \Rightarrow M$$

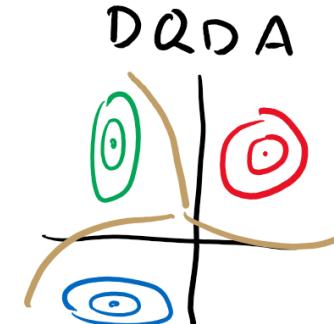
$$P(Y=M) = \pi_M = \frac{N_M}{N}$$

$$P(Y=K) = \pi_K = \frac{N_K}{N}$$

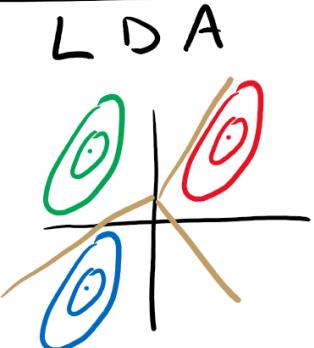
$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$



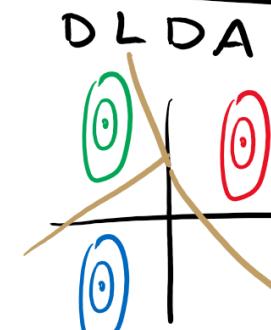
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



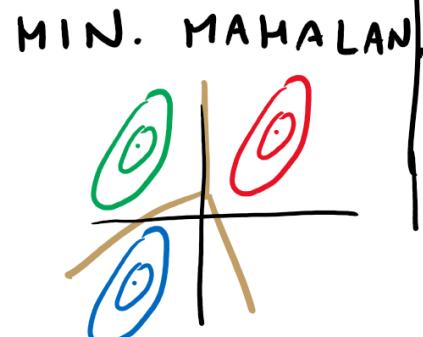
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 & & \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



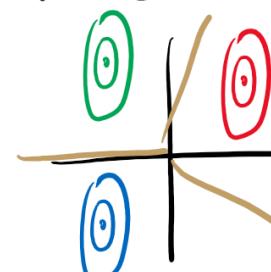
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 & & \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 & & \\ \Pi_1 = \Pi_2 = \Pi_3 & & \end{array}$$

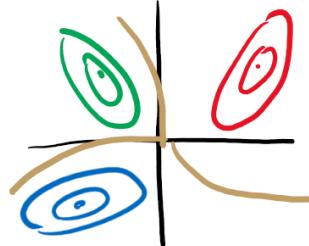


$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 & & \\ \Pi_1 = \Pi_2 = \Pi_3 & & \end{array}$$



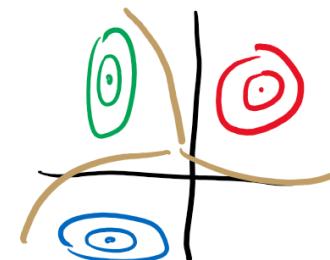
$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

QDA



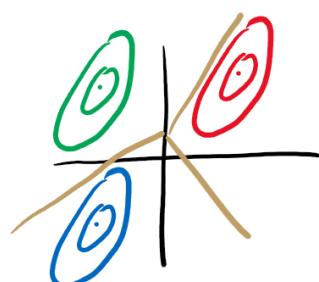
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$

DQDA



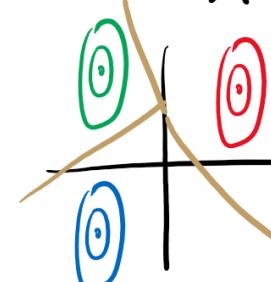
LDA

$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



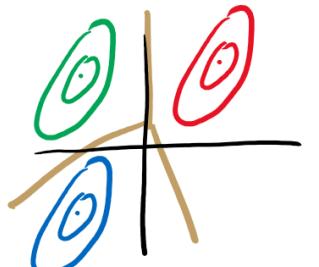
DLDA

$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



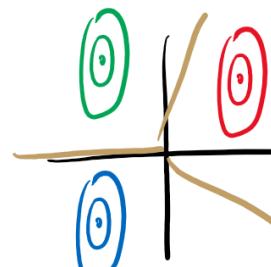
MIN. MAHALAN.

$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 = \Pi_2 = \Pi_3 \end{array}$$

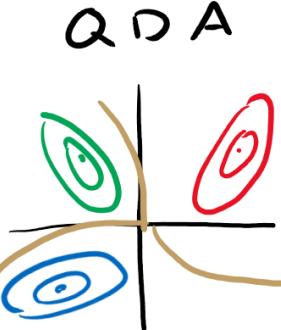


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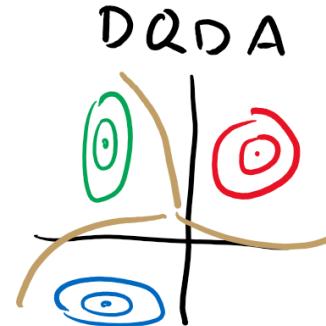
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 = \Pi_2 = \Pi_3 \end{array}$$



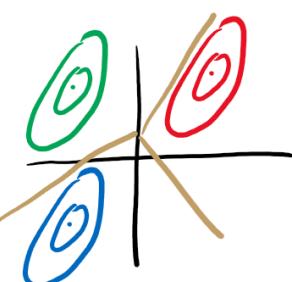
$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$



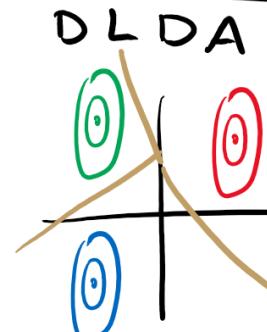
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



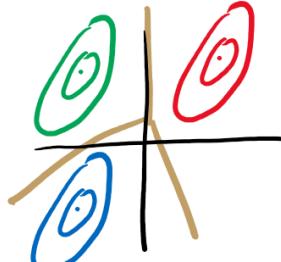
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



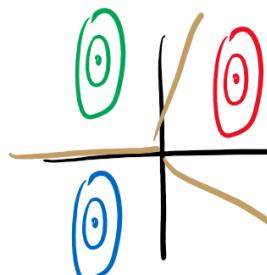
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 & \Pi_2 & \Pi_3 \end{array}$$



$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 = \Pi_2 = \Pi_3 \end{array}$$



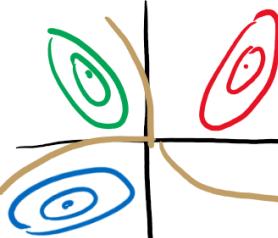
$$\begin{array}{ccc} M_1 & M_2 & M_3 \\ \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \Pi_1 = \Pi_2 = \Pi_3 \end{array}$$



$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

$$\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix}$$

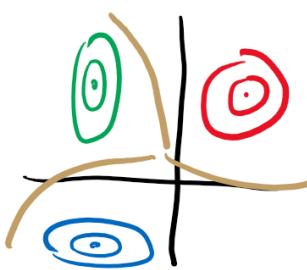
QDA



$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

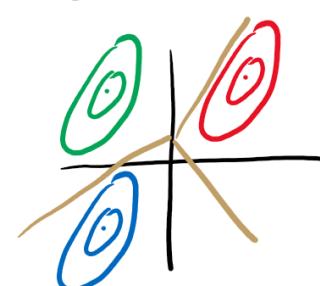
$$\Sigma = \begin{bmatrix} \Sigma_{11} & 0 \\ 0 & \Sigma_{22} \end{bmatrix}$$

DQDA

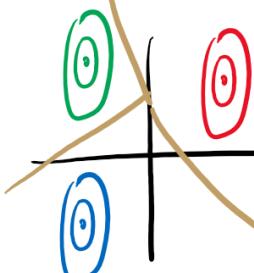


LDA

$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

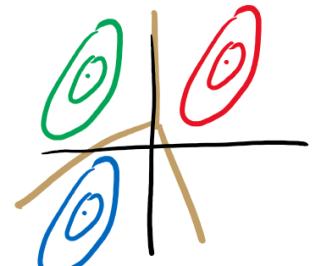


DLDA

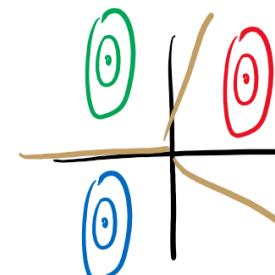


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$$\begin{array}{|c|c|c|} \hline M_1 & M_2 & M_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 = \Pi_2 = \Pi_3 \\ \hline \end{array}$$



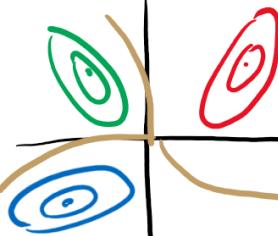
MIN. W. EUKLIDE



$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

$$\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix}$$

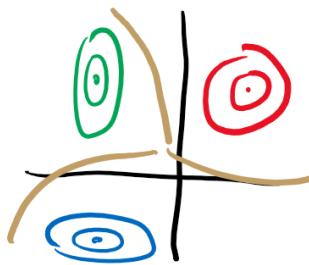
QDA



$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

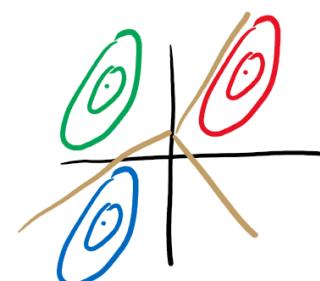
$$\Sigma = \begin{bmatrix} \Sigma_{11} & 0 \\ 0 & \Sigma_{22} \end{bmatrix}$$

DQDA



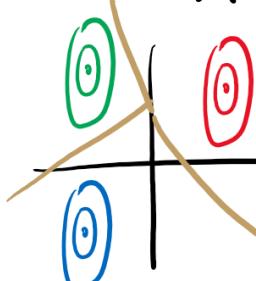
LDA

$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

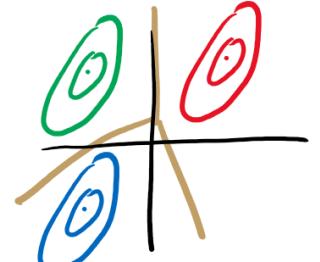


$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

DLDA

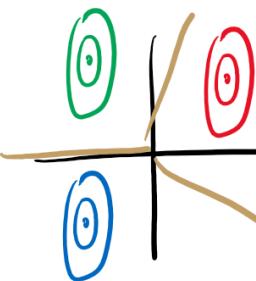


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$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 = \Pi_2 = \Pi_3 \\ \hline \end{array}$$

MIN. W. EUKLIDE

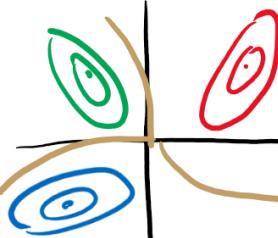


$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 = \Pi_2 = \Pi_3 \\ \hline \end{array}$$

$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

$$\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} \\ \Sigma_{21} & \Sigma_{22} \end{bmatrix}$$

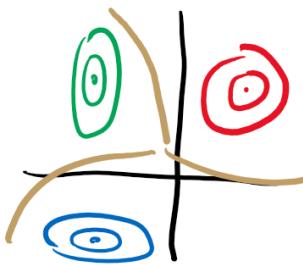
QDA



$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 & \Sigma_2 & \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

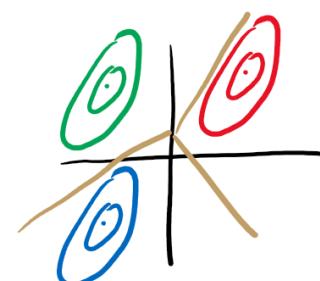
$$\Sigma = \begin{bmatrix} \Sigma_{11} & 0 \\ 0 & \Sigma_{22} \end{bmatrix}$$

DQDA



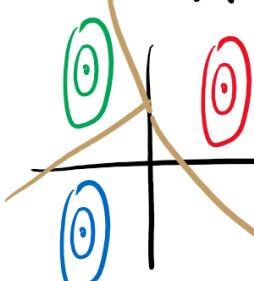
LDA

$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$



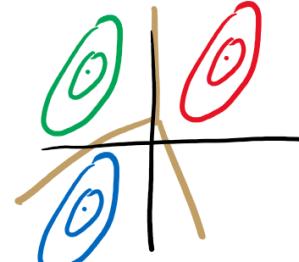
$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 & \Pi_2 & \Pi_3 \\ \hline \end{array}$$

DLDA



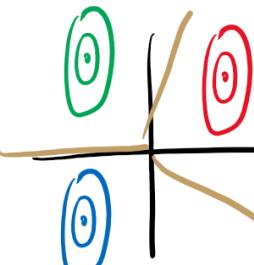
MIN. MAHALAN.

$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 = \Pi_2 = \Pi_3 \\ \hline \end{array}$$

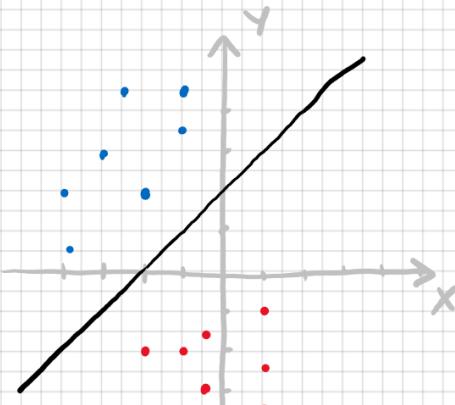


MIN. W. EUKLIDE

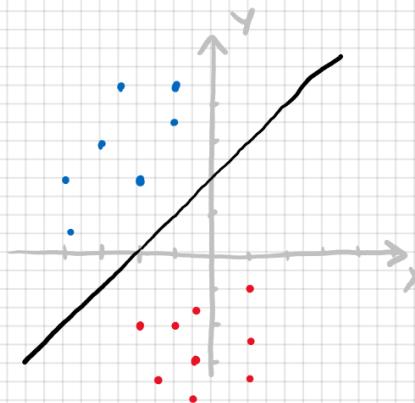
$$\begin{array}{|c|c|c|} \hline m_1 & m_2 & m_3 \\ \hline \Sigma_1 = \Sigma_2 = \Sigma_3 \\ \hline \Pi_1 = \Pi_2 = \Pi_3 \\ \hline \end{array}$$



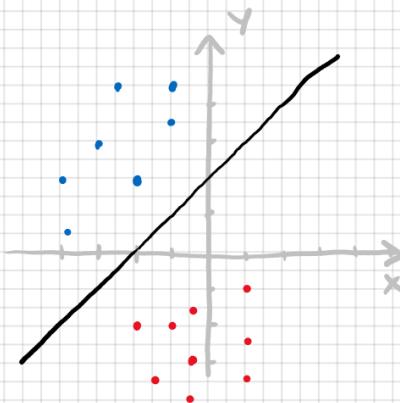
$$y = \alpha x + b$$



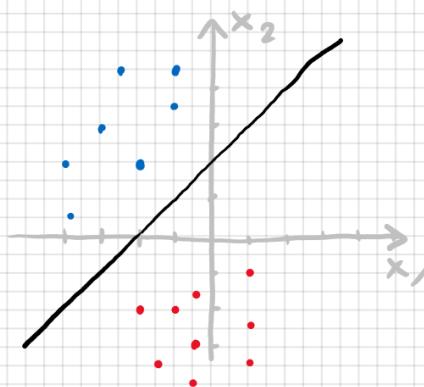
$$2x - y + b = \emptyset$$

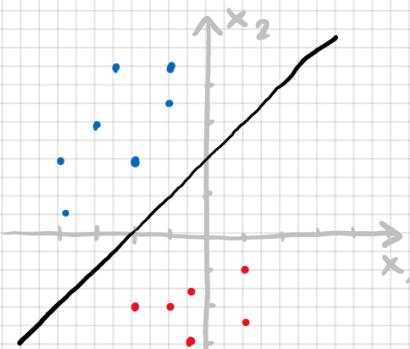


$$w_1x + w_2y + w_0 = \phi$$



$$\omega_1 x_1 + \omega_2 x_2 + w_0 = \phi$$



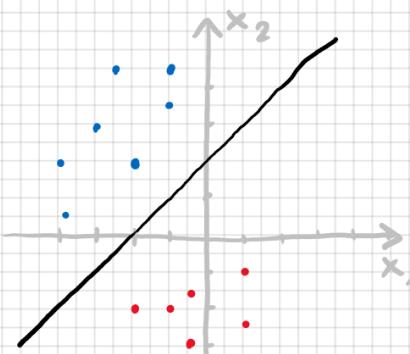


$$\underbrace{w_1 x_1 + w_2 x_2 + w_0 = \phi}_{w^T \cdot x + w_0 = \phi}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$w_0$$

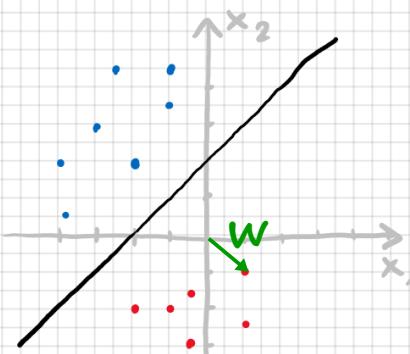


$$\underbrace{w_1 x_1 + w_2 x_2 + w_0 = \phi}_{w^T \cdot x + w_0 = \phi}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$w_0 = 2$$



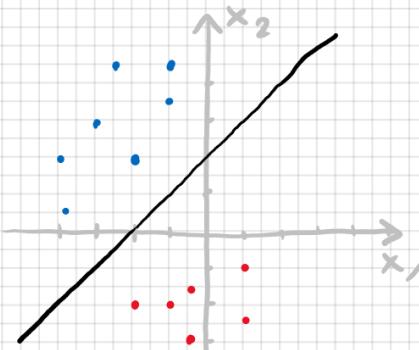
$$w_1 x_1 + w_2 x_2 + w_0 = 0$$

$$w^T \cdot x + w_0 = 0$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$w_0 = 2$$



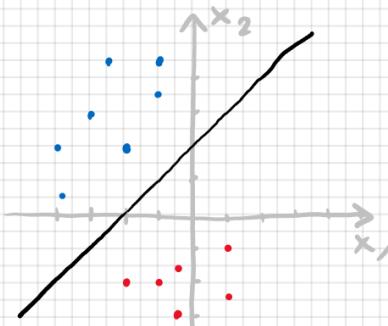
$$\underbrace{w_1 x_1 + w_2 x_2 + w_0 = \phi}_{w^T \cdot x + w_0 = \phi}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$w_0 = 2$$

$$\delta(x) = w_1 x_1 + w_2 x_2 + w_0$$



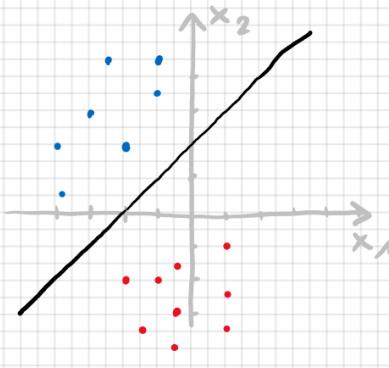
$$\underbrace{w_1 x_1 + w_2 x_2 + w_0 = \phi}_{w^T \cdot x + w_0 = \phi}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -2 \\ -2 \end{bmatrix}$$

$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$w_0 = 2$$

$$\delta(x) = w_1 x_1 + w_2 x_2 + w_0 \Rightarrow \delta(x) = 1 \cdot (-2) + (-1) \cdot (-2) + 2 = 2$$



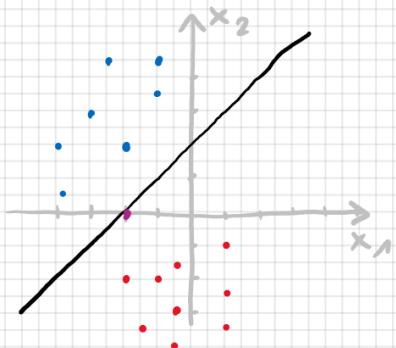
$$\underbrace{w_1 x_1 + w_2 x_2 + w_0 = 0}_{w^T \cdot x + w_0 = 0}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -2 \\ 2 \end{bmatrix}$$

$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$w_0 = 2$$

$$\delta(x) = w_1 x_1 + w_2 x_2 + w_0 \Rightarrow \delta(x) = 1 \cdot (-2) + (-1) \cdot 2 + 2 = -2$$



$$\underbrace{w_1 x_1 + w_2 x_2 + w_0 = 0}_{w^T \cdot x + w_0 = 0}$$

$$x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -2 \\ 0 \end{bmatrix}$$

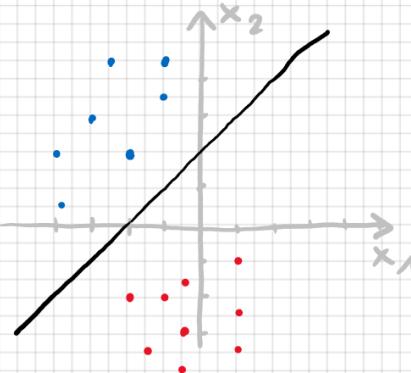
$$w = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

$$w_0 = 2$$

$$\delta(x) = w_1 x_1 + w_2 x_2 + w_0 \Rightarrow \delta(x) = 1 \cdot (-2) + (-1) \cdot 0 + 2 = 0$$

$$\delta(x) = w_1x_1 + w_2x_2 + w_0$$

$$d(x) = \text{sign}(\delta(x)) = \begin{cases} 1 & \Leftrightarrow \delta(x) > 0 \\ -1 & \Leftrightarrow \delta(x) \leq 0 \end{cases}$$



$$\delta(x) = w_1x_1 + w_2x_2 + w_0$$

$$d(x) = \text{sign}(\delta(x)) = \begin{cases} 1 & \Leftrightarrow \delta(x) > 0 \\ -1 & \Leftrightarrow \delta(x) \leq 0 \end{cases}$$

